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**QUEST FOR THE MAGNETIC POLES: RELOCATION OF THE SOUTH  
MAGNETIC POLE AT SEA, 1986.**

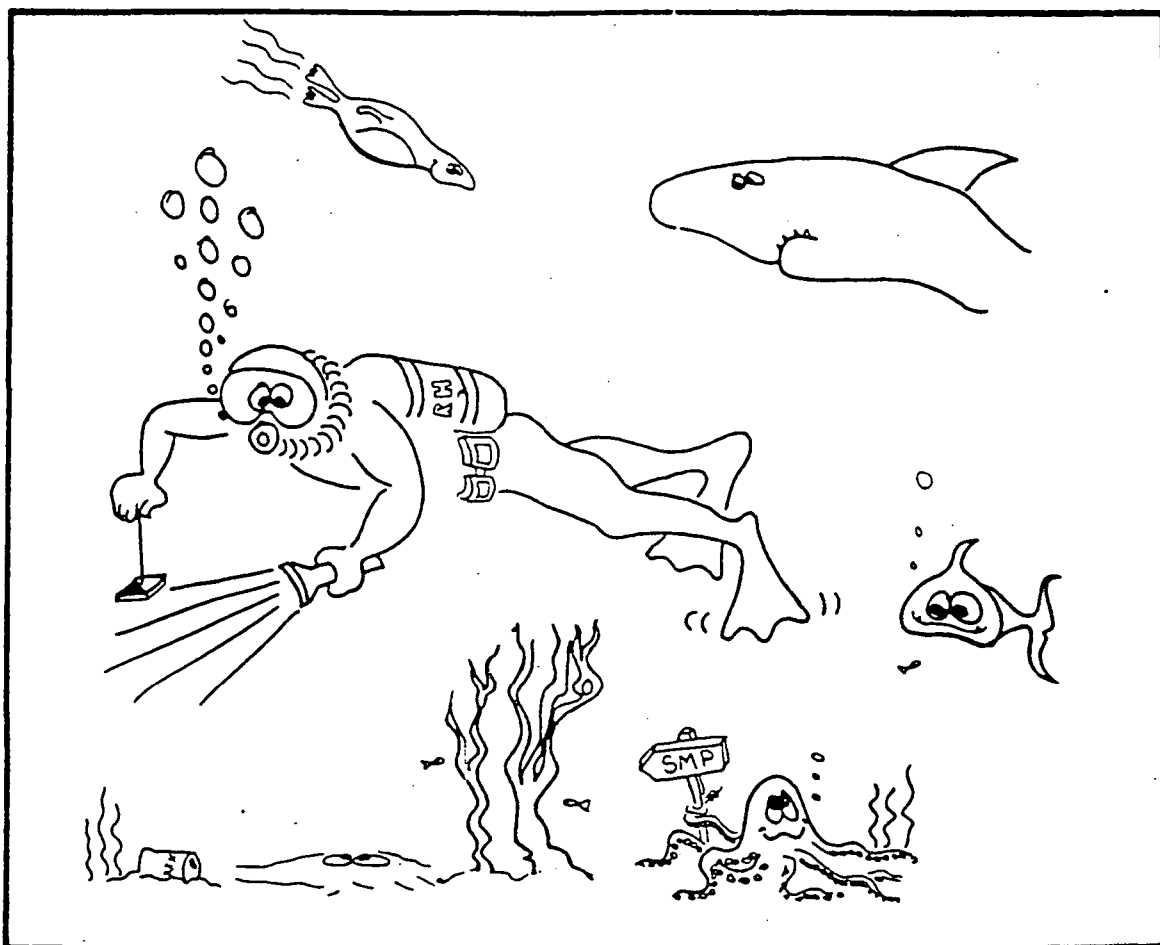
C.E. Barton , R. Hutchinson , P. Quilty , K. Seers and T. Stone .

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1987/3



QUEST FOR THE MAGNETIC POLES: RELOCATION OF THE SOUTH  
MAGNETIC POLE AT SEA, 1986.



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## Abstract

There is a rich and interesting history relating to the exploration for the South Magnetic Pole (SMP), in which Australians have played a leading role. The present location of the South Magnetic Pole (SMP) in the Southern Ocean provides an opportunity to determine its position well-removed from local (coastal) anomalies.

At 03:24 hrs Universal Time (12:44 hrs local meridian time) on 6th January 1986, the position of the SMP was calculated to be latitude  $65^{\circ}19.0'$  S, longitude  $139^{\circ}18.2'$  E. Observations of the magnitude and direction of the horizontal intensity of the geomagnetic field were made from onboard the Australian Antarctic charter vessel *Icebird* which was 11.3 km from the pole when the above position was determined. Not enough observations were made to calculate the mean position of the SMP, although it was estimated to be at approximately  $65^{\circ}20'$  S,  $139^{\circ}10'$  E, i.e. about half a degree south of the dip pole for IGRF 1985 at epoch 1986.0. This places the pole offshore about 150 km north-northwest of the French Antarctic base of Dumont d'Urville, 2750 km from the South Geographic Pole and 1800 km from the South Geomagnetic Pole. The average drift rate of the SMP since 1841 is about 9 km/yr.

This is the first time that the position of either of the magnetic poles has been determined directly (i.e. at close proximity) from a ship and the closest-ever observed approach to the SMP. The three previous direct determinations of the position of the SMP, made on the Antarctic icecap remote from local anomalies, were by Douglas Mawson in 1909, Eric Webb in 1912 and Pierre Mayaud in 1952. The SMP passed close to Dumont d'Urville when it migrated out to sea 30 years ago.

## Introduction

During the second half of the 19th century and the early part of the 20th century there was tremendous interest in terrestrial magnetism, due largely to its importance for navigation. The discovery of the magnetic poles was considered a target for exploration almost equal in importance to that of the geographic poles. Both magnetic poles were the object of a succession of major polar expeditions, and both were reached before their respective geographical counterparts:

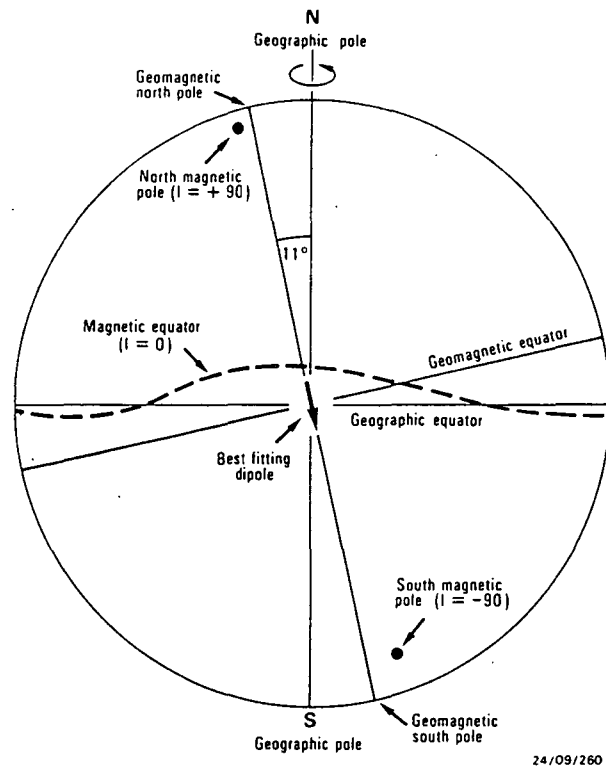
<i>Pole</i>	<i>Date</i>	<i>Leader</i>
North Magnetic Pole	31 May 1831	James Clark Ross
North Geographic Pole	6 Apr 1909	Robert Peary
South Magnetic Pole	16 Jan 1909	Edgeworth David, Douglas Mawson
South Geographic Pole	14 Dec 1911	Roald Amundsen

A knowledge of the position of the magnetic poles is of practical value for chart production and navigation, whereas the secular and diurnal motions of the magnetic poles provide information about the nature of internal and external sources of the magnetic field. Australia has strong historical links with the exploration for the South Magnetic Pole.

## Magnetic and geomagnetic poles

The magnetic poles, or dip poles as they are often called, are the principal points on the globe where the Earth's magnetic field points vertically upwards (the South Magnetic Pole, SMP), and vertically downwards (the North Magnetic Pole, NMP). The horizontal intensity of the geomagnetic field ( $H$ ) at the magnetic poles is, of course, zero. This condition may also occur in the vicinity of intense localized magnetic field anomalies, but such cases are discounted.

The north and south geomagnetic poles are determined by the intersection with the Earth's surface of the geocentric magnetic dipole axis of the Earth. These are antipodal by definition, and may be many thousands of kilometers from the NMP and SMP respectively (Figure 1). The geomagnetic poles are based on a mathematical concept, and are determined from a spherical harmonic analysis of observations of the geomagnetic field taken over the whole surface of the globe. The magnetic poles, on the other hand, have a physical manifestation - namely  $H = 0$ . The geocentric coordinates of the South Geomagnetic Pole for epoch 1986.0, i.e. 1st January 1986, given by the International Geomagnetic Reference Field (IGRF, 1985 revision) are  $79^{\circ}01.4'$  S,  $109^{\circ}04.9'$  E, which is a distance of 1226 km from the South Geographic Pole. The corresponding location of the southern IGRF dip pole is  $64^{\circ}43.3'$  S,  $139^{\circ}10.0'$  E, which is 1859 km from the South Geomagnetic Pole and 2822 km from the South Geographic Pole.



**Figure 1.** Schematic of the magnetic and geomagnetic poles of the Earth. The inclination of the field ( $I$ ) is zero at the magnetic equator and  $+90^\circ/-90^\circ$  at the north and south magnetic poles respectively. The magnetic dipole axis of the Earth is presently inclined at  $11^\circ$  to the geographic axis. Redrawn from McElhinny (1973).

### Movement of the magnetic poles

The magnetic poles drift gradually, and independently, in response to slow changes in convection patterns of molten iron in the core of the Earth. Drift rates are typically a few km/yr, and have increased by an order of magnitude during the last 150 years (see Dawson and Newitt, 1982). For example, the average drift rate for the NMP has been:

0.9 km/yr from 1831 - 1904,  
 2.95 km/yr from 1831 - 1947,  
 7.76 km/yr from 1904 - 1947, and  
 $\approx 25$  km/yr just prior to 1981.

The magnetic poles usually remain within about 20 degrees of the geomagnetic poles.

Superimposed on this secular motion is a rapid daily motion caused by time varying external magnetic fields produced by electric currents in the ionosphere and magnetosphere. The elliptical paths traced out daily by each of the magnetic poles have diameters ranging from less than 10km on magnetically quiet days (Figure 2) to many hundreds of kilometers when the Earth's magnetic field is highly disturbed by emissions from the Sun. At polar latitudes the magnetic field is usually undisturbed for only a few days per month. Hence it is practically impossible to reach an instantaneous position of either of the magnetic poles. A "direct" determination of the position of a magnetic pole may be considered to be one made within 100 km of the pole (McGregor et al., 1982). Accounts of the movement of the Earth's magnetic dip poles and geomagnetic poles during the last 400 years are given by Dawson and Newitt (1982) and McGregor et al. (1982).

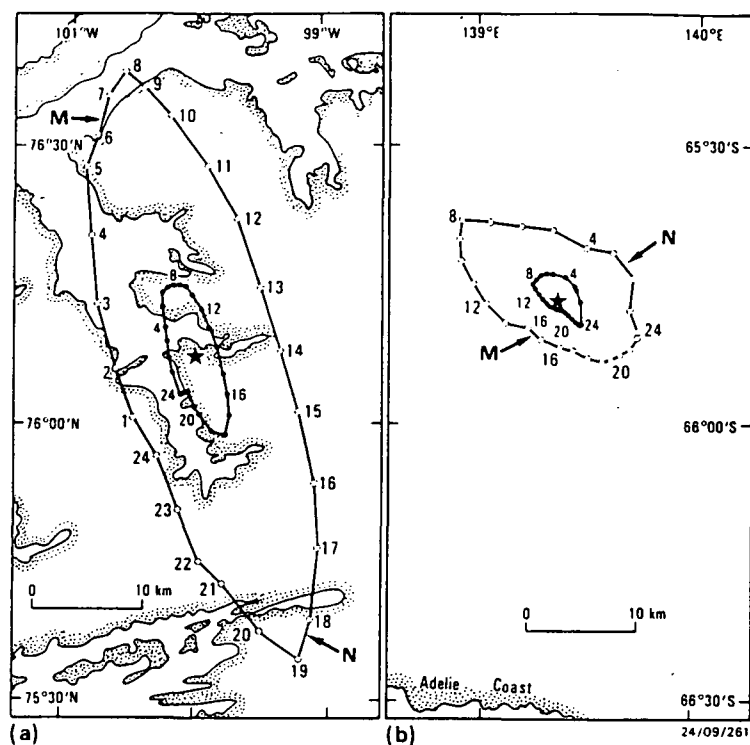


Figure 2. Diurnal paths of (a) the NMP and (b) the SMP in 1975. Closed and open circles denote the average quiet-day paths and disturbed day paths respectively; stars shown the mean positions of the poles; numbers denote hours Universal Time; M & N shown local midnight and noon respectively. Redrawn from Dawson and Newitt (1982, figure 2)

### Discovery of the North Magnetic Pole.

The first attempt to chart the position of the NMP was in 1546 by Geraldus Mercator (of Mercator projection fame). He based his result on magnetic compass directions recorded in the northern hemisphere and the mistaken, but common belief that compasses always point towards the magnetic pole. The location Mercator gave was near the Bering Strait - much too far to the west. He must have realized his model was a poor representation of the observations, for on his world map of 1569 Mercator showed two magnetic north poles. The astronomer and geomagnetician Edmond Halley (1683) adopted a similar view more than a century later:

*"The whole Globe of the Earth is one great Magnet having Four Magnetical poles, or points of attraction, near each pole of the Equator Two; and that, in those parts of the World which lye near adjacent to any one of those Magnetical poles, the Needle is governed thereby, the nearest pole being always predominant over the remote"*

Halley placed the two northern magnetic poles at 75° N, 120° W and "not above" 83° N, 5° W, and the two southern magnetic poles at 74° S, 95° W and 70° S 120° E.

In an attempt in 1615 to locate the coveted Northwest Passage, the English explorer William Baffin, aboard the sailing vessel *Discovery* (the first of a series of polar vessels of that name), was halted by pack ice at 78° N. There he recorded a magnetic declination of 56°. Without knowing it, Baffin must have passed very close to the NMP. However, it was not until 1818 that the quest for the NMP began in earnest. The explorers who featured most prominently in this effort were John Ross and his nephew James Clark Ross, Edward Parry, Edward Sabine, and John Franklin.

James Clark Ross, who maintained a lifelong interest in terrestrial magnetism, was the first person to set foot at the NMP, and still holds the record for the highest inclination observation ever recorded near either magnetic pole ( $89^{\circ} 59'$ ). The expedition was under the command of John Ross and sponsored by Felix Booth, a distillery magnate and Sheriff of the City of London. Ross' vessel *Victory* was handicapped by a monstrous steam engine, the first to be used for polar exploration, which had a maximum speed of 3 knots. As a consequence of their slow progress the expedition was trapped in the ice at  $69^{\circ} 59' \text{ N}$  in Felix Harbour on Boothia Peninsula for two successive winters. Ross calculated the approximate position of the NMP and set off with a sledge expedition along the southwest coast of Boothia Felix. On 31st May 1831 he reached the NMP at  $70^{\circ} 53' \text{ N}$ ,  $96^{\circ} 46' \text{ W}$ . After remaining icebound for a third winter the expeditioners finally abandoned the *Victory*, and were subsequently rescued from Lancaster Sound four months later.

The second direct determination of the position of the NMP was by the Norwegian, Roald Amundsen, during his 1903-1907 expedition that successfully located the coveted Northwest passage. Amundsen made an extended set of observations and operated a magnetic observatory on King William Island for 2 years. He was able to demonstrate that the daily motion of the pole was along an elliptical path, and gave the mean position of the NMP for 1904 as  $70^{\circ} 30' \text{ N}$ ,  $95^{\circ} 30' \text{ W}$ . Since 1831 the pole had moved some 66 km at an average speed of 0.9 km/yr, which is more than an order of magnitude slower than today.

The position of the North Magnetic Pole is now monitored routinely by the Canadian Department of Energy Mines and Resources, Division of Seismology and Geomagnetism. Historical summaries of the search for the NMP are given by Serson (1981, 1982).

### Discovery of the South Magnetic Pole

Shortly after Ross' visit to the NMP the German physicist Carl Friedrich Gauss predicted that the SMP would be at  $66^{\circ} \text{ S}$ ,  $146^{\circ} \text{ E}$ . His prediction was based on results of the first spherical harmonic analysis of worldwide observations of the field. To polar explorers this provided an irresistible challenge, particularly as nobody had succeeded in reaching this region of the globe.

Expeditions to discover the SMP by the French explorer Jules Sebastian César Dumont d'Urville aboard the *Astrolabe* in 1840, and the American Lieutenant Charles Wilkes in 1838-1840 were successful in exploring much of the coast of East Antarctica (Adélie Land and Wilkes Land). However, they were only able to establish that the SMP must be to the east of the position predicted by Gauss.

On 30th September 1839 James Clark Ross set out from London with two vessels, the *Erebus* and the *Terror*, on what was to be the last of the great polar sailing voyages. His object was to plant the flag he had taken to the NMP at the SMP. While in Hobart visiting Sir John Franklin, who had been appointed the Governor of Tasmania, Ross heard of the discoveries of Dumont d'Urville and Wilkes and resolved to attempt to penetrate the pack ice further to the east. This proved to be remarkably successful and resulted in his discovery of the sea and island named after him (with its two volcanoes, Erebus and Terror named after the ships). He succeeded in penetrating further south than any previous attempt, and opened up the approach used by Shackleton, Amundsen and Scott to the geographic pole. Ross found his passage to the magnetic pole barred by the Trans-Antarctic Mountain chain. His final observations from Ross Island ( $78^{\circ} \text{ S}$ ,  $168^{\circ} \text{ E}$ ) in 1841 indicated the SMP to be some 250 km to the west.

Interest in polar exploration waned until the start of the 20th century. Expeditions by Robert F. Scott aboard the *Discovery* (1901-1904) and Erich von Drygalski aboard the *Gauss* (1901-1903) were no more successful than Ross in getting closer to the magnetic pole, but did make extensive measurements from Cape Adare down the western coast of the Ross Sea. [The *Gauss* was specially built for Drygalski's expedition under the sponsorship of Dr Alexander von Neumayer, who spent many years in Australia as Director of the Melbourne Observatory, and conducted the first detailed magnetic survey of the Colony of Victoria.]

The first, and successful overland attempt to reach the magnetic pole was in 1909 during Shackleton's British Antarctic Expedition, 1907-1909. The objectives of the expedition were to reach both the geographic and magnetic poles from their base at Cape Royds on Ross Island, and to explore the land to the east of the Ross Sea. The SMP party comprised Prof. Tannatt William Edgeworth David from Sydney University (leader, until he relinquished this role to Mawson in the final days of the journey), Douglas Mawson from the University of Adelaide (cartographer and magnetic observer), and the Scotsman Alistaire Mackay (medical doctor). The party carried the following magnetic instruments:

one	3"	Cary compass-theodolite	(for sun and declination observations)
two	2.5"	Brunton prismatic compasses	(which performed excellently)
one	6"	Trough needle	(to determine declination)
one		Lloyd-Creak Dip Circle	(for determining inclination and total intensity)

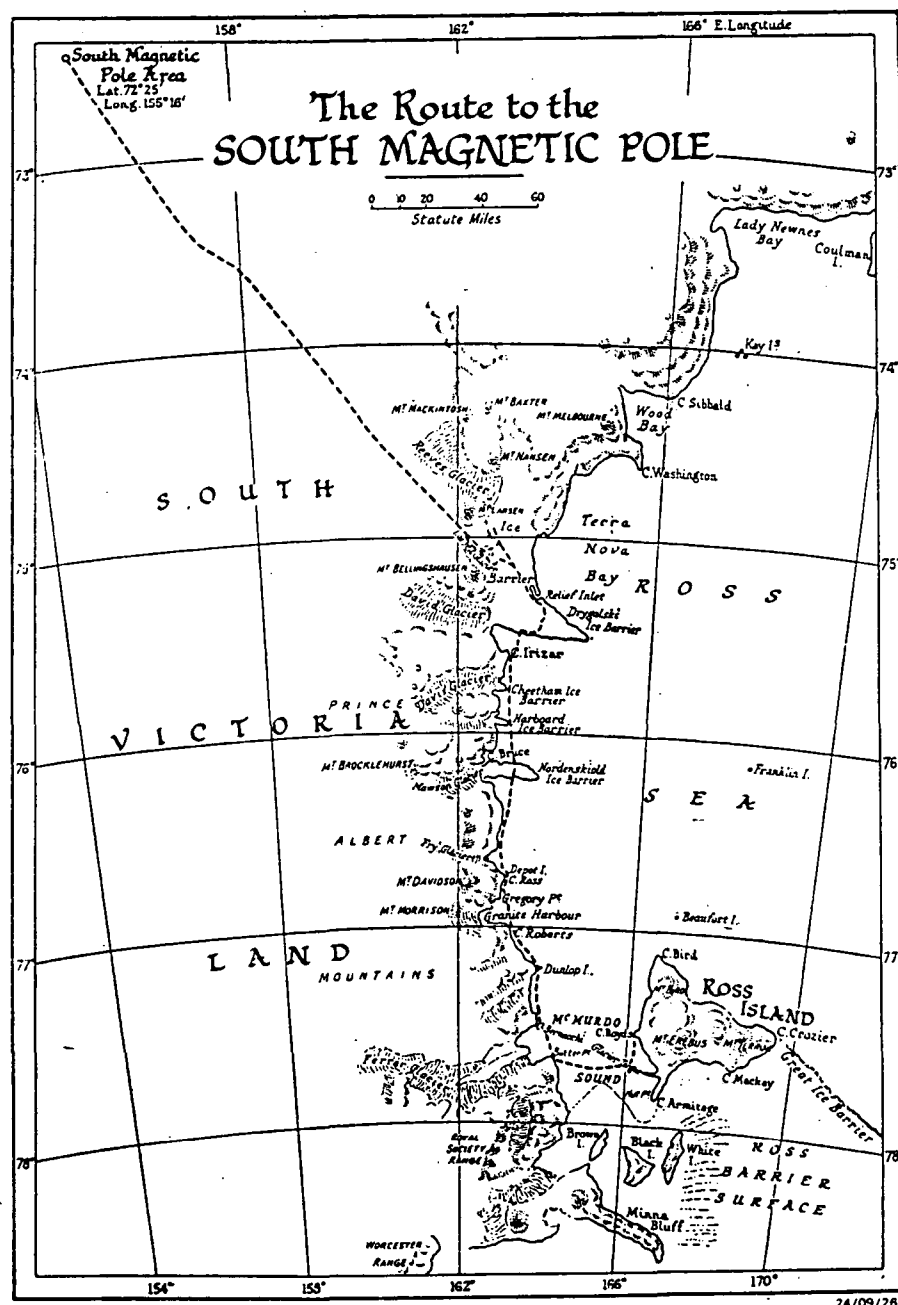


Figure 3. Route to the South Magnetic Pole followed by T.W.E. David, D. Mawson and A.F. Mackay to the SMP, October 1908 - January 1909.

Shackleton had come armed with the first motor vehicle to be used in Antarctica, a 12-15 hp air-cooled New Arrol-Johnston. Despite some injuries inflicted on the SMP party in their attempts to keep this beast mobile (Mackay sustained a broken wrist), it did manage to establish depots at 10 km and 15 km. Beyond that the party was obliged to man-haul their 2 tons of equipment on two sledges, named the 'Christmas Tree' and 'Plum Duff' after their appearance and contents respectively. The weight of the sledges and the nature of the terrain required working in relays dragging a single sledge at a time. In this manner progress was limited to a mere 6.5 km/day under good conditions. They advanced 390 km northwards along the western coast of the Ross Sea to reach Relief Inlet, north of the Drygalski Ice Barrier on 12th December 1908 (Figure 3). The difficulties they encountered can be gauged from the 2 weeks taken to cross this 32 km wide ice tongue. Here they depôted the Christmas Tree sledge before heading across the mountains and inland to the 2000m plateau. It was already clear that their chances of reaching the magnetic pole and returning to the coast in time to be picked up by the *Nimrod* before the end of January were slender.

On 15th January Mawson observed a dip of  $89^{\circ} 45'$ , and suggested waiting for the pole to drift towards the party. However, they agreed to force march the remaining 21 km the following day to Mawson's calculated mean position of the pole, and return 18 km. This was an undertaking of no mean daring considering the nature of the weather and the exhausted condition of the party. Their efforts were rewarded, and on 16th January 1909 at 3.30 pm the Union Jack was hoisted at the calculated mean position of the magnetic pole at  $72^{\circ} 25' S$ ,  $155^{\circ} 16' E$  (Figure 4), with the previously rehearsed proclamation by Prof. David: "I hereby take possession of this area now containing the Magnetic Pole for the British Empire". They managed to cover the 400 km return journey to Depot Inlet in 18 days, and by great good fortune on the following day, 4th February, were sighted and picked up by the *Nimrod*.

Thus the SMP was reached 3 months before Peary reached the North Geographic Pole, and 3 years to the day before Robert Falcon Scott was to arrive at the South Geographic Pole, only to discover Amundsen's success four weeks before. David, Mawson and Mackay's epic 2000 km man-hauled sledge journey to the SMP remains one of the most remarkable feats of Antarctic exploration.



Figure 4. T.W.E. David, D. Mawson and A.F. Mackay at the South Magnetic Pole, 16 January 1909.

The second visit to the SMP was made in 1912 by Eric Norman Webb during Mawson's 1911-1914 Australasian Antarctic Expedition. Webb was a dedicated geomagnetician and made extensive observations of the field, both at the expedition's base on Cape Denison at Commonwealth Bay and during the sledge journey to the magnetic pole with Captain Robert Bage (officer in charge) and Captain Frank Hurley. The steepest inclination recorded by Webb was  $-89^{\circ}43.3'$  on 21st December 1912, at the party's most southerly observation point (station 7). Webb estimated from his previous observations that the rate of change of inclination with distance towards the pole was 0.23 minutes of arc/km. Thus they were about 62 km from the SMP. Both Webb and Mawson fully appreciated that it was impossible to determine accurately the mean position of the magnetic pole without making an extensive set of observations spanning many weeks.

Webb analysed and published Mawson's results as well as his own (Webb and Chree, 1925). He pointed out that Mawson's final calculation of the position of the magnetic pole was based on incomplete sets of dip circle observations made during the final stage of the journey to the magnetic pole (a full set of observations is tedious, even under ideal conditions, and was impractical under the conditions and time constraints that Mawson suffered). Based on estimated corrections to Mawson's data, Webb concluded that the magnetic pole must have been approximately 130 km northwest of the position reached by David, Mawson and Mackay.

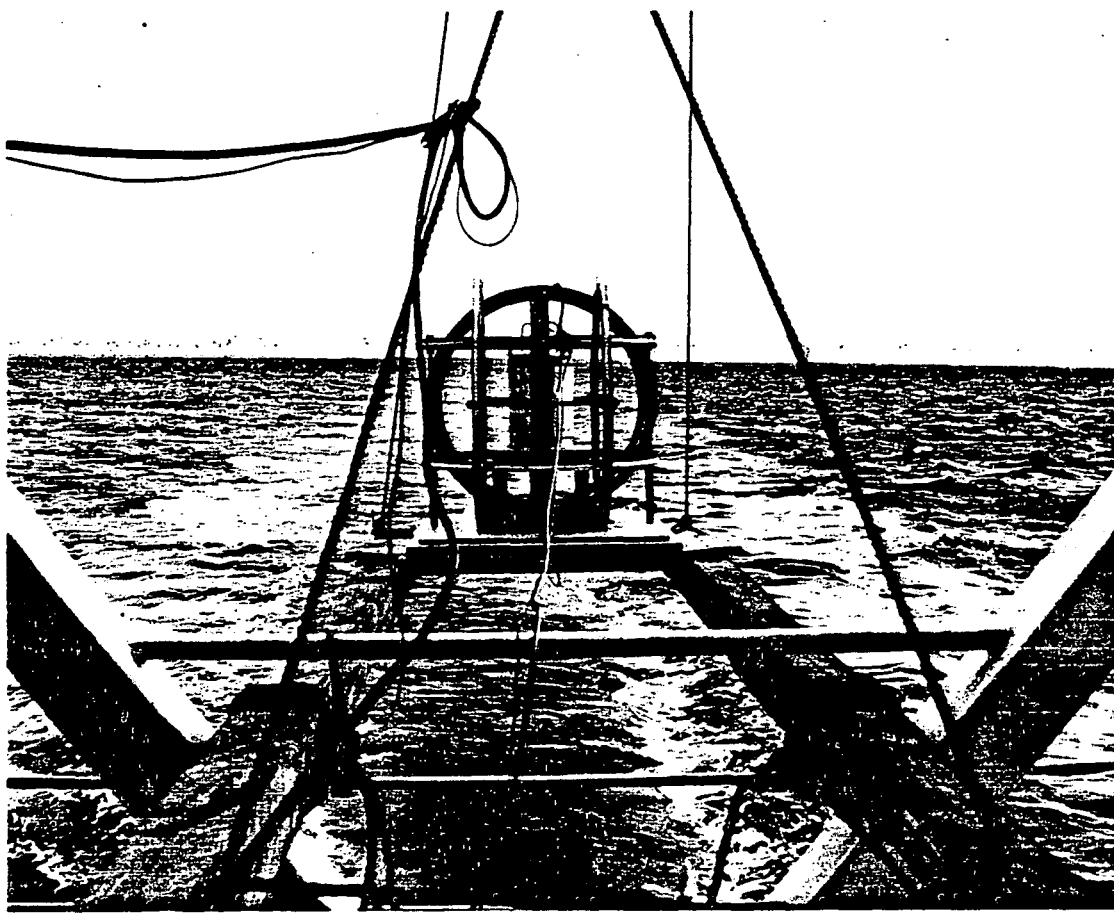
No further effort was made to reach the SMP for the next 40 years, although Vestine et al. (1947) published a set of global maps of the geomagnetic field with SMP positions for 1922, 1932, 1942 and 1945. The last close approach to the SMP was in 1952 by Pierre-Nöel Mayaud during the French Antarctic Expedition to Adélie Land. Magnetic observations were made in the vicinity of base at Port Martin and at Cape Denison, Commonwealth Bay, and at stations a short distance inland on the plateau. Based on the new and previous observations, Mayaud (1953) estimated the position of the magnetic pole to be  $68^{\circ}7'S$ ,  $143.0^{\circ}E$ . The nearest station to the SMP was the one 10 km south of Cape Denison, at a distance of 116 km.

Observations made at coastal stations are difficult to interpret directly because of the effects of local magnetic anomalies. For example, mean values of the field recorded at the magnetic observatory at Dumont d'Urville point to an apparent position of the SMP nearly 100 km to the east of its true position. The mean position of the SMP passed close to Dumont d'Urville when it drifted off the continent 30 years ago (Figure 9b), and the instantaneous position of the SMP must have passed through the station on many occasions during its transient daily motion. Observations made at sea and on thick ice on the Antarctic plateau are relatively isolated from the problem of local magnetic anomalies.

### Location of the SMP, January 1986

In January 1986 the Antarctic Division's charter vessel *Icebird* passed within the vicinity of the SMP going to and from Commonwealth Bay. The opportunity was taken to redetermine the location of the pole directly using a specially developed fluxgate magnetometer system that permitted shipboard measurements of  $H$ .

The sensor comprised two 3" Kelvin-Hughes fluxgate probes mounted at right-angles on a gimbal bearing so as to remain in the horizontal plane. This was fitted inside a sealed non-magnetic aluminium vessel designed for ocean-bottom use. A ballast weight with damping fins was attached to the gimbal and the whole container filled with oil. Considerable trial and error with the viscosity of the oil was required to obtain optimum (critical) damping. The sealed sensor unit was mounted at the centre of an orthogonal set of three 1 m diameter Helmholtz coils to provide compensation for the magnetic effect of the vessel. The whole assembly was bolted to a wooden boom protruding 2 m from the stern of *Icebird*, and about 5 m above the waterline (Figure 5). The "A" and "B" fluxgates were aligned along the reverse sternwards axis of the vessel and to port respectively.



**Figure 5.** Fluxgate sensor unit and Helmholtz coil assembly mounted on wooden beams extending from the stern of *Icebird*, photographed in the vicinity of the South Magnetic Pole

The fluxgate control unit was a 3-channel EDA magnetometer (EDA Electronics, Toronto, Canada) with a sensitivity of 1 VDC per 100 nT. A 5-position attenuator was fitted to reduce the sensitivity. Ranges and calibration figures are summarized in Table 1. Only the 10 000 and 20 000 nT range settings were used in practice. In order to obtain an integrated output from each channel, the two output signals were passed through a voltage-to-frequency converter that sent a train of pulses to a counter and 6-digit display. A frequency offset was included to avoid resolution problems around zero volts:

$$\text{Output frequency (Hz)} = 500 V + 5000$$

where V is the EDA fluxgate output voltage for a given channel. A hand operated switch was used to latch the two digital displays and restarted the integration counters.

Ship positions were determined with the onboard Magnavox MX 1142 satellite navigation system. This system provided a fix every hour (on average) with a precision of 100 m. Errors in the ship's speed affect the accuracy. According to the system handbook, accumulated errors after 2 hours should give a position accurate to within 1.6 km under most conditions at sea.

Table 1 Fluxgate attenuator settings and calibration figures

Switch position	Nominal range (nT)	Calibration figure (nT/volt)	
		Channel A	Channel B
1	$\pm 1000$	102.3	102.6
2	$\pm 2000$	200.0	201.0
3	$\pm 5000$	487.3	490.0
4	$\pm 10000$	959.4	959.4
5	$\pm 20000$	1895.1	1918.8

### Compensation for the ship's field

The Helmholtz coils, powered by separate constant current power supplies, were used to provide first-order cancellation of the magnetic influence of the vessel. On the approach to the SMP (at  $62^{\circ} 22' S$ ,  $141^{\circ} 54' E$  on 01 Jan 86, 20:12 UT) the currents in the Helmholtz coils were adjusted to null the field at the sensors with *Icebird* pointing along (B channel adjustment) and at right angles (A channel adjustment) to the magnetic meridian, as determined by the ship's magnetic compass. Declination was  $20^{\circ} E$  at this point and the field of the vessel at the sensors in the forward direction was approximately 7000 nT. This simple compensation procedure turned out to be adequate, although better compensation could have been achieved by zeroing the averages of the appropriate sensor signals for the vessel pointing both forward and backwards along the meridian and transverse directions.

The magnetization induced in steel vessels by the Earth's magnetic field is commonly of the same order of magnitude as the permanent (remanent) magnetization, and must therefore be considered. In the vicinity of a magnetic pole the horizontal component of the geomagnetic field is small and we need concern ourselves only with induction by the vertical component. Because of the shape anisotropy of susceptibility of the ship, this will produce a horizontal field at the magnetometer. However, this will be virtually independent of the direction in which the ship is pointing and will effectively be a constant addition to the remanent magnetization component. Provided the cancellation procedure described above is performed close to the magnetic pole, no further correction is required. The observational technique used (below) was designed to give second-order cancellation of the magnetic effect of the ship.

### Observational technique

Determinations of  $H$  in the region of the pole were made by sailing the vessel in a tight circle at approximately constant angular speed. Signals from the A and B fluxgates (backwards and to port) were integrated over successive  $20^{\circ}$  sectors and converted to components along two fixed axes in space (X and Y) for each of the 18 sectors. When these components are averaged over a complete spin the residual field of the vessel cancels out and the magnitude and direction of  $H$  is obtained (Appendix A). Reduction of the sector size will improve the finite element approximations involved. It is convenient, but not necessary, for the reference axes X and Y to be geographic north and east.

For a purely dipolar field the rate of change of  $H$  with distance from the pole is 4.69 nT/km (for IGRF 1986.0), and the rate of change of inclination is 0.27 minutes of arc/km (Appendix B). Direct observations of the rate of change of inclination with distance from the South Magnetic Pole were made by Eric Webb in 1912, and integrated with the 1909 data and results from earlier indirect observations to obtain an isoclinic chart for the region (Webb and Chree, 1925; reproduced

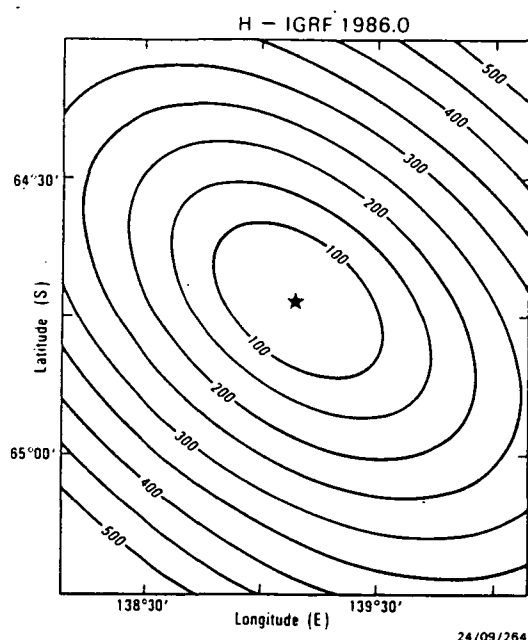


Figure 6. Horizontal intensity of the magnetic field around the southern dip pole for epoch 1986.0 given by IGRF 1985. The coordinates of the dip pole are  $64^{\circ} 43.3' \text{ S}$ ,  $139^{\circ} 10.0' \text{ E}$ .

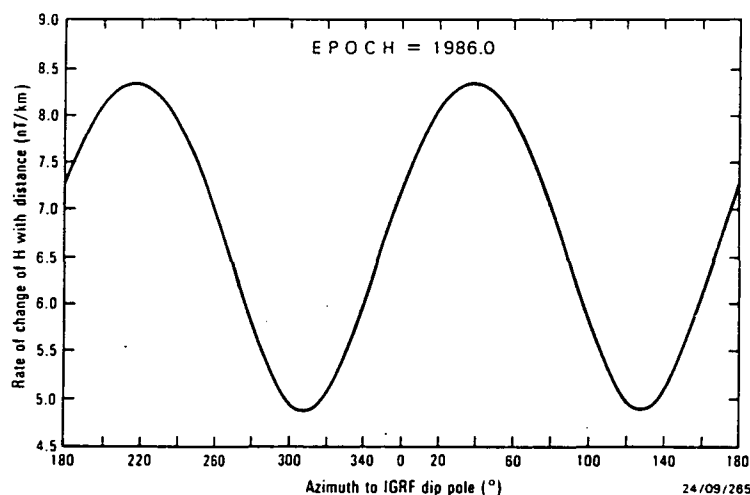
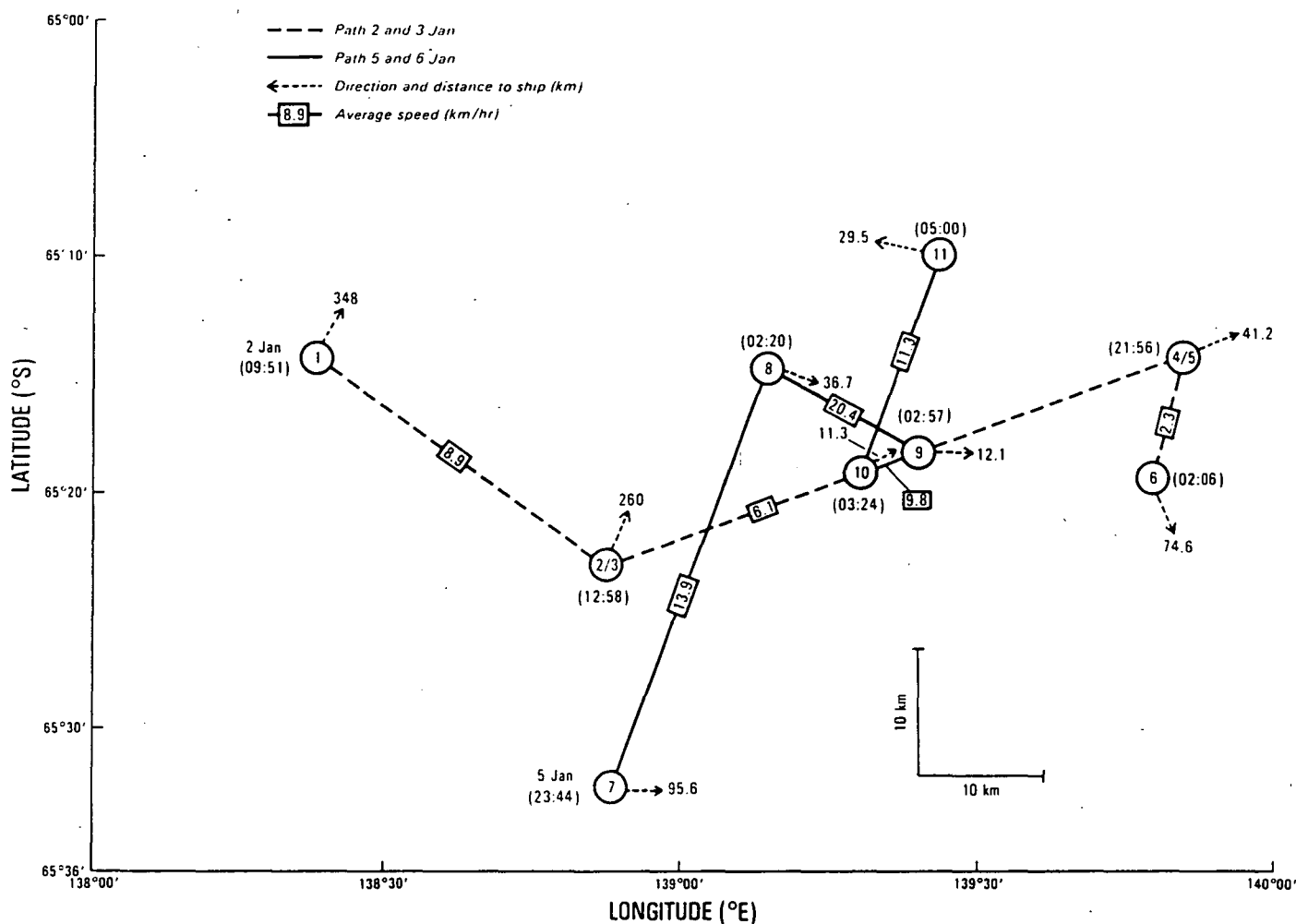


Figure 7. Rate of change of  $H$  with distance as a function of true bearing towards the dip pole for epoch 1986.0 given by IGRF 1985. Ordinate values are averaged over a radial distance of  $1^{\circ}$ . Distances are measured on a sphere on radius 6371.2 km.

in Burrows, 1963). During the final stage of Eric Webb's journey inclination was observed to change at 0.235 minutes of arc/km, which is equivalent to a rate of change of  $H$  of 4.72 nT/km for a dipole field model. For the purpose of preliminary reduction of observations, a value of 4.7 nT/km for the rate of change of  $H$  with distance was used.

Final data reduction was based on the 1986.0 pattern of the field given by IGRF 1985 (Figure 6), assuming that the observed vector  $H$  always points exactly away from the instantaneous position of the SMP. The rate of change of  $H$  with distance as a function of azimuth (Figure 7) is



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Figure 8. Observed positions (circled numbers) of the South Magnetic Pole on 2-3rd January (joined by dashed line) and 5-6th January 1986 (joined by solid lines). Average speeds of the SMP between spins are shown boxed in the joining lines. Double arrows denote the direction and distance to the ship when observations were made. Times of observations (UT) are shown in parenthesis beside each pole position. Observations 2/3 and 4/5 are averages of two consecutive spins.

considerably higher than for the dipole model, and can be modelled to better than 3-figure accuracy by:

$$\frac{dH}{ds} = 6.7124 - .0184 \cos z + .0018 \sin z + .4196 \cos 2z + 1.6611 \sin 2z \\ - .0073 \cos 3z + .0142 \sin 3z + .0980 \cos 4z - .0528 \sin 4z \\ + .0022 \cos 5z + .0004 \sin 5z - .0098 \cos 6z - .0107 \sin 6z$$

where  $z$  is the azimuth relative to geographic north measured towards the dip pole. The actual pattern of the geomagnetic field in the region of the SMP has not changed substantially during this century (as noted by Vestine et al., 1947).

## Results

Positions of the ship, observed values of  $H$ , distances from the SMP and inferred coordinates of the SMP are given in Table 2 and plotted in Figure 8. Note that distances are

TABLE 2. Summary of SMP observations

SPIN NO.	UT DATE	UT TIME (hr:min)	SHIP'S POSITION		H (nT)	BEARING TO SMP (deg)	DISTANCE AWAY (km)	SMP POSTITION		MOVEMENT km	AV SPEED km/hr
			LATITUDE (North)	LONGITUDE (East)				LATITUDE	LONGITUDE		
1	2 Jan	09:51	-62°30.0'	141°50.0'	2864	207.5	348	-65°14.2'	138°23.0'	27.8 @ 8.9 48.9 @ 6.1 9.8 @ 2.3	
2/3	2 Jan	12:58	-63°20.2'	141°28.6'	2148	207.7	260	-65°23.1'	138°52.0'		
4/5	2 Jan	22:00	-65°05.9'	140°40.5'	309	248.4	41.2	-65°14.0'	139°51.2'		
6	3 Jan	02:06	-65°57.0'	140°21.9'	446	339.2	74.6	-65°19.3'	139°47.6'		
7	5 Jan	23:44	-65°36.0'	140°58.0'	597	272.8	95.6	-65°32.6'	138°53.0'	33.8 @ 13.9 12.6 @ 20.4 4.4 @ 9.8 18.1 @ 11.3	
8	6 Jan	02:20	-65°21.7'	139°54.0'	202	285.7	36.7	-65°15.6'	139°8.9'		
9	6 Jan	02:57	-65°18.3'	139°39.7'	76	271.6	12.1	-65°18.1'	139°24.1'		
10	6 Jan	03:24	-65°16.7'	139°31.7'	86	247.2	11.3	-65°19.0'	139°18.2'		
11	6 Jan	05:00	-65°06.5'	138°49.0'	168	102.3	29.5	-65°9.8'	139°26.0'		

Results for consecutive pairs of spins

2	2 Jan	12:54	-63°20.2'	141°28.6'	2148	208.5	260	-65°22.1'	138°48.0'	3.8	
3	2 Jan	13:02	-63°20.2'	141°28.6'	2148	207.5	261	-65°23.8'	138°52.4'		
4	2 Jan	21:52	-65°5.9'	140°40.5'	249	244.9	32.2	-65°13.2'	140°2.9'	18.2	
5	2 Jan	22:00	-65°5.9'	140°40.5'	370	252.0	49.9	-65°14.0'	139°39.4'		

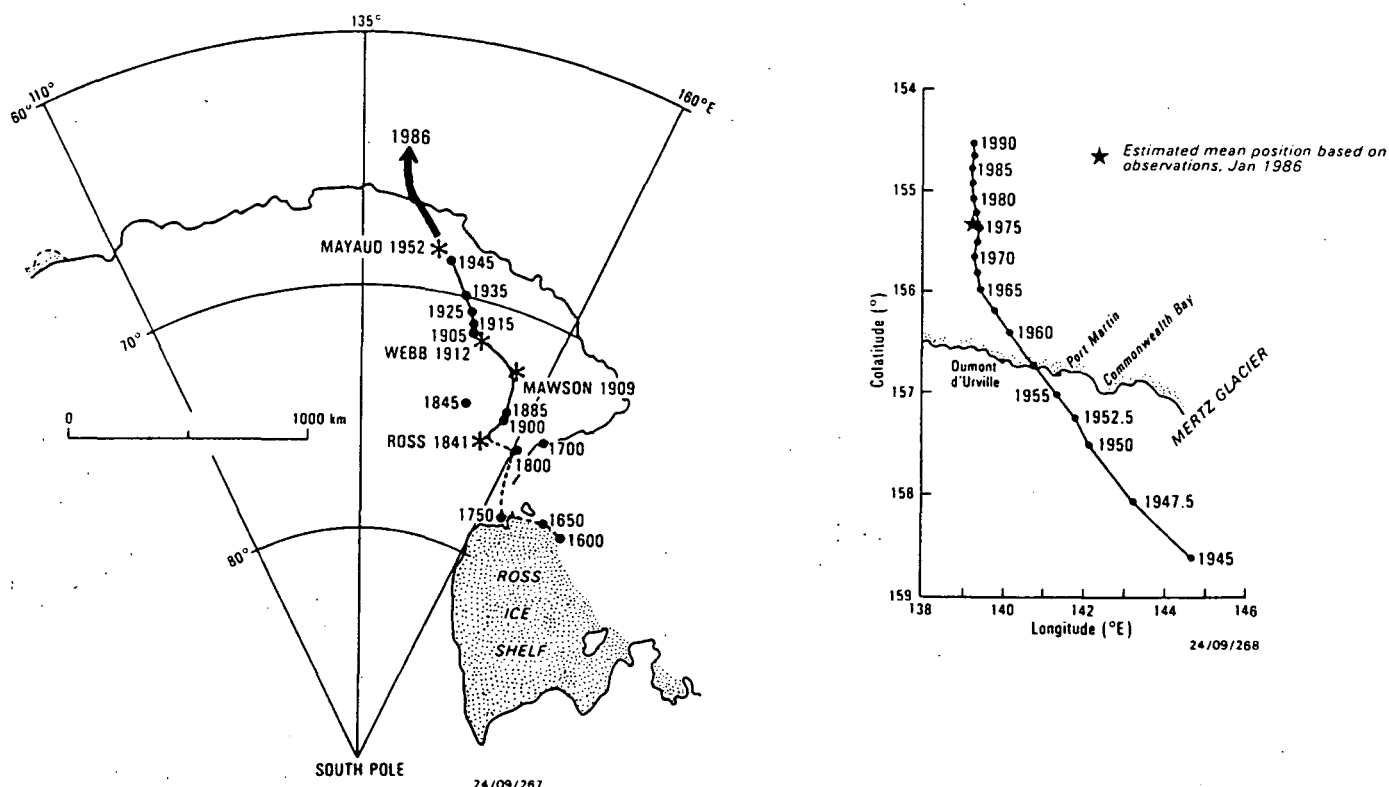
calculated for a spherical Earth of radius 6371.2 km (i.e. they are really a measure of the angle subtended at the centre of the Earth). Entries in the table for spins 2/3 and 4/5 are the means for these consecutive pairs of spins. Spin numbers 1,2 and 3 were made more than 200 km from the pole are not considered to be reliable, despite the excellent agreement between consecutive spins 2 and 3. The closest observed distance to the pole was 11.3 km for spin number 10 made at 03:24 hrs UT on 6th January 1986 (12:44 hrs local meridian time). Pole positions for the two pairs of spins differ by 3.8 km and 18.2 km respectively. This provides a measure of the uncertainty in the method. The effects of errors (particularly in the true bearing of the pole) become smaller as we approach the magnetic pole, and could be reduced substantially by averaging over many spins. There was not enough ship-time available to do this.

Average speeds of the SMP calculated between spins range from a few km/hr to a few tens of km/hr (Table 2). This is consistent with the moderate level of geomagnetic activity which prevailed on 2/3rd January and on 5/6th January 1986.

## Conclusion

The position of the SMP has been determined directly (i.e. from close proximity) by ship-board observations of the horizontal component of the Earth's magnetic field made on 2/3rd January and 5/6th January 1986. The closest observed approach to the SMP was 11.3 km at 03:24 hrs UT, 6th January, when the magnetic pole was calculated to be at  $65^{\circ} 19.0' \text{ S}$ ,  $139^{\circ} 18.2' \text{ E}$ .

Not enough observations were made during either of the two intervals of measurements to permit the mean position of the SMP to be calculated. However, the general sense and orientation of the pole path are consistent with that inferred indirectly by Dawson and Newitt (1982) from means of observatory data (Figure 2b). This suggests that the mean position of the magnetic pole is in the vicinity of  $65^{\circ} 20' \text{ S}$ ,  $139^{\circ} 10' \text{ E}$ . The southern dip pole for IGRF 1985 at epoch 1986 is at  $64^{\circ} 43.3' \text{ S}$ ,  $139^{\circ} 10.0' \text{ E}$ , i.e. about half a degree to the north. Successive southern dip pole positions for the IGRF (1985 revision) are shown on Figure 9b, and indicate that the pole drifted off the continent between Dumont d'Urville and Port Martin in about 1957.



**Figure 9. (a)** Movement of the South Magnetic Pole since 1600 A.D. Asterisks denote direct determinations, as defined in the text (including Ross' position for 1841); solid circles denote determinations based on charts and extrapolation from remote observations; the thick line is the SMP path given by the IGRF model, as detailed in (b). [Part (a) modified from McGregor et al., 1982].

This is the first time that either of the magnetic poles has been located directly from onboard a ship. If we take Webb's corrections to Mawson's observations in 1912 (Webb and Chree, 1925), then this is also the closest observed approach to the SMP. Previous "direct" determinations of the position of the SMP were made by Mawson in 1909, Webb in 1912 and Mayaud in 1952.

Movement of the SMP since 1600 A.D. is illustrated in Figure 9. Direct determinations (asterisks - including that of James Clark Ross in 1841) are combined with positions determined from remote observations and charts (solid circles) and the IGRF (open circles and inset). Since 1841 the SMP has drifted 1300 km in a north-northwesterly direction at an average speed of about 9 km/yr. Since 1952 its average drift rate has been about 10 km/yr. It is currently approximately 154 km offshore from the French Antarctic base of Dumont d'Urville in a north-northwesterly direction, 2750 km from the south geographic pole, and 1800 km from the South Geomagnetic Pole.

C.F. Gauss would be pleased to know that his prediction of the position of the SMP made in the 1930's is now in error by less than 300 km.

### Acknowledgements

We thank the Captain and crew of *Icebird* for their cooperation and the Antarctic Division for logistic support. A. White loaned ocean-bottom magnetometer components, P.A. Hopgood calibrated the fluxgates, J. Bitterly and J. Folques, Institut de Physique du Globe, Strasbourg provided data from Dumont d'Urville, and P.L. McFadden generated the harmonic model of the IGRF dH/ds curve. This paper is published with the permission of the Director, Bureau of Mineral Resources, Geology and Geophysics.

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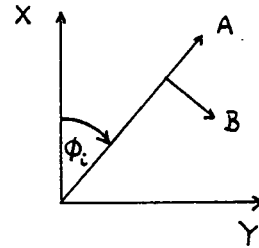
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## APPENDIX A - Theory of the observational technique.

Let  $X, Y$  = arbitrary horizontal axes in space (geographic north and east are convenient)  
 $A, B$  = stern-wards and port axes of the ship  
 $H_X, H_Y$  = horizontal components of the field along the  $X$  and  $Y$  axes  
 $\beta$  = size of each integration section (degrees), e.g.  $10^\circ$  or  $20^\circ$   
 $N_A, N_B$  = sum of the counts of the  $A$  and  $B$  channel integrators

Consider the ship spinning about a vertical axis at constant angular speed. We divide each spin into an even number of small sectors, of size  $\beta$  (typically  $10^\circ$  or  $20^\circ$  in practice). Let  $\phi_i$  be the angle between the  $X$  and  $A$  axes for the middle of the  $i$ th sector of the spin, and let the first sector start at  $\phi=0$  and time  $t=0$  (see sketch opposite).

Then



$$\phi_i = (i-1)\beta + \beta/2 = \beta(i - 1/2) \quad \dots\dots\dots (1)$$

As discussed in the text, the output of the voltage-frequency converter (in Hz) for a particular channel is given by

$$\begin{aligned} f_{\text{out}} &= 500 V + 5000 \\ &= 500 H/k + 5000 \end{aligned}$$

where  $V$  is the output voltage of the EDA fluxgate,  $k$  is the calibration figure in nT/volt (see Table 1), and  $H$  is the field along the axis of the fluxgate. The mean value of the frequency for time interval  $t$  during which the counter accumulates  $N$  pulses is  $N/t$ .

Hence for the  $i$ th sector, the mean values of  $H$  in nT for the  $A$  and  $B$  channels are given by

$$\begin{aligned} H_{Ai} &= (N_{Ai}/t_i - 5000) / 500 k \\ H_{Bi} &= (N_{Bi}/t_i - 5000) / 500 k \end{aligned} \quad \dots\dots\dots (2)$$

These have components along the  $X$  and  $Y$  axes given by

$$X_i = H_{Ai} \cos \phi_i - H_{Bi} \sin \phi_i \quad \dots\dots\dots (3)$$

and

$$Y_i = H_{Ai} \sin \phi_i + H_{Bi} \cos \phi_i$$

However, if  $S_A$  and  $S_B$  are the components of the magnetic field of the ship along the  $A$  and  $B$  axes, and  $H_X$  and  $H_Y$  are the horizontal components of the Earth's field along the  $X$  and  $Y$  axes, then to a first approximation for small sector sizes ( $\beta$ ),

$$X_i = H_X + S_A \cos \phi_i - S_B \sin \phi_i \quad \dots\dots\dots (4)$$

and

$$Y_i = H_Y + S_A \sin \phi_i + S_B \cos \phi_i$$

$S_A$  and  $S_B$  are constant, so when summed over one complete spin of the vessel comprising an even number of sectors ( $n=360/\beta$ ), the  $\sin$  and  $\cos$  terms become zero.

Hence 
$$H_X = \frac{1}{n} \sum_i (X_i) = \frac{1}{n} \sum_i (H_{Ai} \cos \phi_i - H_{Bi} \sin \phi_i)$$

and 
$$H_Y = \frac{1}{n} \sum_i (Y_i) = \frac{1}{n} \sum_i (H_{Ai} \sin \phi_i + H_{Bi} \cos \phi_i)$$

Finally, the horizontal component of the Earth's field is of magnitude  $H_E = \sqrt{H_X^2 + H_Y^2}$  at angle  $\tan^{-1}(H_Y/H_X)$  clockwise from the X axis.

Integrating the signals over finite sectors introduces approximations into equations (3) and (4), but these is not important provided the sectors are fairly small, e.g.  $10^\circ$  or  $20^\circ$ . By extending the integration over a finite number of spins (N) the signal-to-noise ratio can be improved by a factor of  $\sqrt{N}$ .

Computer programs SMP85 and MAGPOLE, written in Microsoft BASIC 2.1 for an Apple Macintosh, are listed below. Program SMP85 performs the above calculations to find  $H_E$ , the true bearing of the pole and the distance to the pole in km (for a 1986.0 IGRF field model). Program MAGPOLE computes magnetic pole coordinates from ship coordinates and the distance and true bearing of the magnetic pole. All coordinates are geocentric and all distances are measured on a sphere of radius 6371.2 km.

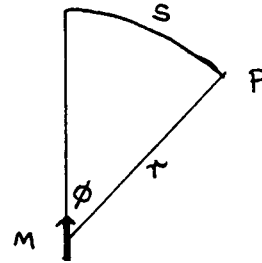
## APPENDIX B - Rate of change of dipole field at a magnetic pole

Consider a point P at radial distance  $r$  and angle  $\varnothing$  (arc length,  $s$ ) from a dipole of moment  $M$  as sketched opposite.

The magnetic potential at P due to M is

$$U = r g_1^0 \cos \varnothing \quad \dots \dots \dots (1)$$

and  $g_1^0 = \frac{\mu_0 M}{4 \pi r^3}$



in SI units where  $\mu_0 = 4\pi \cdot 10^{-7}$  H/m, and  $g_1^0$  is the spherical harmonic Gauss coefficient representing the axial dipole contribution to the magnetic potential. The tangential component of the field is given by the appropriate partial derivative of  $U$ , namely

$$H = - \frac{\partial U}{\partial s} = - \frac{\partial U}{\partial \varnothing} \cdot \frac{\partial \varnothing}{\partial s} = - \frac{1}{r} \frac{\partial U}{\partial \varnothing} = g_1^0 \sin \varnothing \quad \dots \dots \dots (2)$$

thus  $\frac{dH}{ds} = \frac{dH}{d\varnothing} \cdot \frac{d\varnothing}{ds} = \frac{g_1^0}{r} \cos \varnothing \quad \dots \dots \dots (3)$

At the geomagnetic poles,  $\cos \varnothing = \pm 1$ , the geocentric radius is 6371.2 km, and  $g_1^0 = 29855$  nT for IGRF 1986.0. Thus the rate of change of the horizontal component of the dipole field with great circle distance is  $\pm 4.69$  nT/km.

From radial and tangential derivatives of equation (1) it follows that the dipole field at a geomagnetic pole ( $F_p$ ) is twice that at the dipole equator, and the latter is equal to  $g_1^0$ . Furthermore, the rate of change with distance of  $F_p$  is equal to  $(g_1^0 \sin \varnothing)/r$  and is therefore zero at each magnetic pole, hence

$$\frac{dI}{dH} = \frac{1}{F_p}$$

and,  $\frac{dI}{ds} = \frac{dI}{dH} \cdot \frac{dH}{ds} = \frac{1}{F_p} \cdot \frac{g_1^0}{r} = \frac{1}{2r}$

Hence the rate of change of magnetic inclination (dip) with distance from a geomagnetic pole is 1/12742 radians/km, i.e. 0.27 minutes of arc/km.

APPENDIX C. Program listings

Program SMP85                      Macintosh MS BASIC 2.1                      Rev: 09 Dec 86

Does 2-axis sector summation for SMP project, using 1985 calibration data

Input:

- B - sector size (deg)
- Ka(5), Kb(5) - sensitivity of A, B channels for each switch setting (nT/V)
- AZ - true bearing of starting, X-axis (deg)
- NA, NB - readings for the A and B channel integration counters
- TS - time interval for each sector (sec)

Output:

- H - horizontal component of Earth's field (nT)
- Hx, Hy - fields along X and Y axes (nT)
- Sa, Sb - residual field of ship along A and B axes (nT)
- DD - true bearing to pole (deg)
- RATE - dH/ds (nT/km) from harmonic model of IGRF85 at epoch 1986.0
- KM - distance to pole in km on sphere of radius 6371.2 km

---

```
CLS
WIDTH 72,9
DPR=45/ATN(1) : RPD=ATN(1)/45
DIM Ka(5),Kb(5)
Ka(1)=102.3 :Ka(2)=2001 :Ka(3)=487.3 :Ka(4)=959.4 :Ka(5)=1895.1
Kb(1)=102.6 :Kb(2)=2011 :Kb(3)=4901 :Kb(4)=959.4 :Kb(5)=1918.8
PRINT : LPRINT
200 PRINT" -----.Program SMP85 -----".PRINT

RAT0=6.7124 :mean dH/ds over 1deg from SMP for IGRF1986 in nT/km
AZ=0 :default true bearing(T.B.) of starting axis

300 INPUT" Sector size (deg)= ";B :Reset parameters
LPRINT" Sector size=";"B;" deg
NS=360/B :number of sectors per spin
INPUT" Attenuator switch position(1-5)= ";SW
PRINT" Sensitivity factor for channel A (nT/V)= ";Ka(SW)
PRINT" Sensitivity factor for channel B (nT/V)= ";Kb(SW)
LPRINT" Sensitivity factor for channel A (nT/V)= ";Ka(SW)
LPRINT" Sensitivity factor for channel B (nT/V)= ";Kb(SW)
INPUT" Record (spin) number= ";NUM
NUM=NUM-1

320 NUM=NUM+1 : PRINT : LPRINT :start next spin
PRINT" Record (spin) number";NUM
LPRINT" Record (spin) number";NUM : LPRINT
INPUT" True bearing (deg) of origin axis (0=no change)= ";AZZ
IF(AZZ<>0) THEN AZ=AZZ
LPRINT" True bearing of origin axis = ";AZ : LPRINT

SUMX=0 :SUMY=0 :SUMA=0 :SUMB=0
FOR I=1 TO NS
BEEP : PRINT : PRINT" Sector number";I
350 INPUT" A counter="; NA
```

```

      INPUT " B.counter="; NB
360  INPUT " Sector time(sec)="; TS
      IF (TS=0) THEN 360
      INPUT " Continue (any key), repeat last entry (R)"; Q$
      IF (Q$="R" OR Q$="r") THEN 350

      HA=(NA/(TS*500)-10)*Ka(SW) : HB=(NB/(TS*500)-10)*Kb(SW)
      A=RPD*B*(1-.5)
      SUMA=SUMA+HA : SUMB=SUMB+HB
      SUMX=SUMX + HA*COS(A) - HB*SIN(A)
      SUMY=SUMY + HA*SIN(A) + HB*COS(A)
NEXT
BEEP : BEEP
HX=SUMX/NS : HY=SUMY/NS           :H compts. along chosen axes
SA=SUMA/NS : SB=SUMB/NS           :Ship's field
H=SQR(HX*HX+HY*HY)
D=DPR*ATN(HY/HX) : IF (HX<0) THEN D=D+180 :Rel. azimuth of H
DD=D-180+AZ : DR=DD*RPD           :True bearing to pole

RATE=RAT0-.0184*COS(DR)+.0018*SIN(DR)+.4196*COS(2*DR)+1.6611*SIN(2*DR)
RATE=RATE-.0073*COS(3*DR)+.0142*SIN(3*DR)+.098*COS(4*DR)-.0528*SIN(4*DR)
RATE=RATE+.0022*COS(5*DR)+.0004*SIN(5*DR)-.0098*COS(6*DR)-.0107*SIN(6*DR)
km=H/RATE

HX=.1*INT(10*HX+.5) : HY=.1*INT(10*HY+.5) :round for printing
SA=.1*INT(10*SA+.5) : SB=.1*INT(10*SB+.5)
H=.1*INT(10*H+.5) : DD=.01*INT(100*DD+.5)
RATE=.001*INT(1000*RATE+.5) : km=.1*INT(10*km+.5)
PRINT
PRINT " Hx=";HX;" Hy=";HY;" Sa=";SA;" Sb=";SB;" nT"
PRINT " H=";H;"nT, T.B. to pole=";DD;"deg, Rate=";RATE;"nT/km, Dist=";km;"km"
PRINT:LPRINT
LPRINT " Hx=";HX;" Hy=";HY;" Sa=";SA;" Sb=";SB;" nT"
LPRINT " H=";H;"nT, T.B. to pole=";DD;"deg, Rate=";RATE;"nT/km, Dist=";km;"km"
LPRINT

900 INPUT " Next spin (N), Reset parameters (R), Quit (Q)"; Q$
PRINT : LPRINT
IF (Q$="n" OR Q$="N") THEN 320 :next spin, same parameters
IF (Q$="r" OR Q$="R") THEN 300 :reset parameters
IF (Q$="q" OR Q$="Q") THEN 999 :Quit
GOTO 900
999 END

```

MAGPOLE

Macintosh MS BASIC 2.1

Rev: 3 Dec 86

'Input: Ship lat.(N), lon.(E), dist. to pole (km), true bearing to pole (E)

'Output: Pole lat (N), lon (E) in deg and deg+mins

'Uses geocentric coordinates, Earth radius=6371.2 km

'Enter angles as +/- deg and mins (mins always positive)

CLS

WIDTH 72,9

DEFSNG A-Z

DEF FNASN(X)=ATN(X/SQR(-X\*X+1))

DEF FNACS(X)=1.570796\*-ATN(X/SQR(1-X\*X))

DPR=45/ATN(1) : RPD=1/DPR

200 PRINT:PRINT"----- Program MAGPOLE -----":PRINT

INPUT" Ship lat (N) degrees="; SLT

INPUT" - - - - - minutes="; SLTM: IF(SLT<0) THEN SLTM=-SLTM

SLT=SLT+SLTM/60

INPUT" Ship long (E) degrees="; SLN

INPUT" - - - - - minutes="; SLNM: IF(SLN<0) THEN SLNM=-SLNM

SLN=SLN+SLNM/60

INPUT" True bearing to pole (degE) ="; DD

INPUT" Distance to magpole (km) ="; XD

D=DD\*RPD : S=(90-SLT)\*RPD : X=XD/6371.2 : S=colat, X= dist. in rad.

P=FNACS(COS(S)\*COS(X)+SIN(S)\*SIN(X)\*COS(D)) : pole colat in rad

A=FNASN(SIN(D)\*SIN(X)/SIN(P)) : polar angle of sph.triangle

PLT=90-(P\*DPR) : PLN=SLN+(A\*DPR) : magpole lat, lon

PLTD=INT(PLT) : PLTM=(PLT-PLTD)\*60

IF(PLTD<0) THEN PLTD=PLTD+1 : PLTM=60-PLTM

PLND=INT(PLN) : PLNM=(PLN-PLND)\*60

IF(PLND<0) THEN PLND=PLND+1 : PLNM=60-PLNM

PRINT: LPRINT

PRINT" Magpole latitude (N) = ";PLT;"deg " ;PLTD;"deg " ;PLTM;"min"

PRINT" Magpole longitude (E)= ";PLN;"deg " ;PLND;"deg " ;PLNM;"min"

LPRINT" Ship lat=";SLT;" lon=";SLN;" deg " Azim=";DD;" deg " Dist=";XD;" km"

LPRINT" Magpole latitude (N) = ";PLT;"deg " ;PLTD;"deg " ;PLTM;"min"

LPRINT" Magpole longitude (E)= ";PLN;"deg " ;PLND;"deg " ;PLNM;"min"

PRINT: LPRINT

INPUT" Repeat (RETURN) or quit (Q)";Q\$

IF(Q\$="q" OR Q\$="Q") THEN END

PRINT: CLS : clear screen

SLTM=0: SLNM=0: DM=0 : clear mins to allow return default=0

GOTO 200 : return for next record

999 END